

Transport Phenomena

Make all possible assumptions and show all your work.

1. (20%) Define and give the physical interpretations of the following terms.

Prandtl mixing length

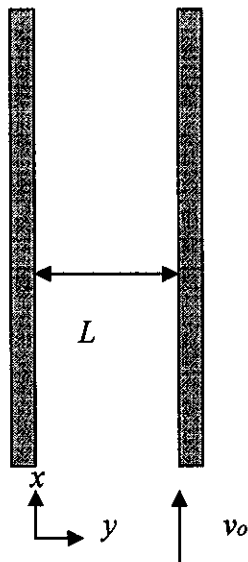
Eddie diffusivity

Reynolds number

Continuum theory

Mach number

2. (15%) Consider an incompressible fluid confined between two parallel, vertical surfaces. One surface, shown to the left, is stationary, while the other is moving upward at a constant velocity, v_0 . If we consider the fluid Newtonian and the flow laminar, derive the velocity profile when the fluid is subject to a pressure gradient $\frac{dP}{dy}$.



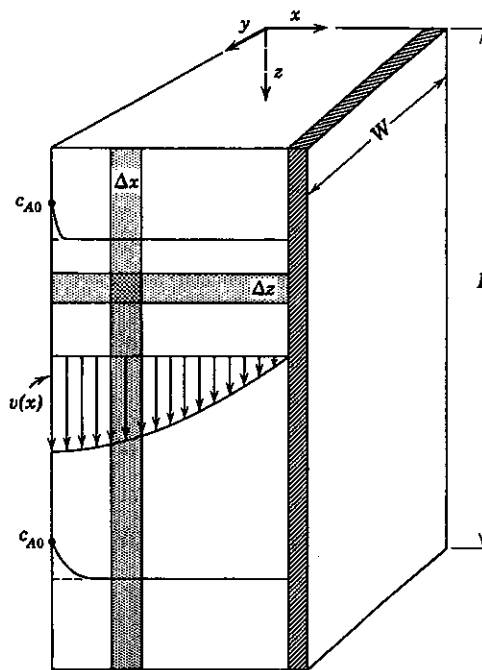
3. (15%) Use the von-Kármán integral method to find the velocity profile, boundary layer thickness, and friction coefficient for the laminar boundary layer over a flat plate by the form $v_x = a \sin by$.

The governing equation can be simplified as $\frac{\tau_o}{\rho} = \frac{d}{dx} \int_0^\delta v_x (v_\infty - v_x)$



4. (25 %) A slab occupying the space between $y = 0$ and $y = b$ is initially at temperature T_0 . At time $t > 0$, the surface at $y = 0$ is suddenly raised to T_1 and maintained there, and the surface at $y = b$ is kept adiabatic. Find the unsteady-state temperature profile $T(y, t)$ within the slab.
5. (25 %) Consider the absorption of gas A by a laminar falling film of liquid B flowing down against a vertical solid wall, as shown below. The thickness and the maximal surface velocity of the falling film are δ and v_{\max} , respectively.

The material A is only slightly soluble in B and the contact time between the fluid and the wall is so short, so that the viscosity μ of the liquid is not changed appreciably and the diffusion takes place very slowly and is confined merely to the gas-liquid interface region. Find the steady state concentration profile of A , $C_A(x, z)$, within the flowing film.



Absorption into a falling film.